

# Dynamic Bandwidth Allocation Schemes to Improve Utilization under Non-Uniform Traffic in Ethernet Passive Optical Networks

Kyuhoo Son\*, Hyungkeun Ryu\*, Song Chong\* and Taewhan Yoo\*\*

\*Department of Electrical Engineering and Computer Science  
Korea Advanced Institute of Science and Technology (KAIST)  
Email: {skio, hkryu}@netsys.kaist.ac.kr, song@ee.kaist.ac.kr

\*\*EPON Team, Network Technology Laboratory  
Electronics and Telecommunications Research Institute (ETRI)  
Email: twyoo@etri.re.kr

**Abstract**—In this paper, conventional bandwidth allocation schemes in Ethernet Passive Optical Network (EPON) are shown to suffer from poor utilization under the non-uniform traffic, particularly as the number of ONUs, guard time and round-trip time increase. To resolve this problem, we propose a new scheme which intelligently allocates a timeslot in consideration of other ONUs' queue occupancy, instead of strictly enforcing maximum timeslot size. The analysis and simulation results show that the proposed scheme can provide significantly higher utilization than the conventional schemes and support max-min fairness under the non-uniform traffic.

## I. INTRODUCTION

Recently the capacity of backbone networks has been increased drastically, but there has been only a little change in access networks. With the rapid growth of the number of users and multimedia services, access networks become bottlenecked. A passive optical network (PON), a point-to-multipoint optical network composed of passive elements without any active elements, is regarded as the most likely technology to solve this problem [1], [2] and considered to be an easy way to implement a fiber-to-the-home (FTTH). Especially Ethernet PON (EPON) is the best candidate for next generation access network because ethernet is cheap, simple and popular [3]. Fig. 1 shows a typical topology of EPON. An optical line terminal (OLT), located at local exchange, is connected with multiple optical network units (ONUs). In downlink transmission from OLT to ONUs, a frame is automatically broadcasted to all ONUs through an optical splitter and each ONU filters the received frame depending on its destination address. In uplink transmission from ONUs to OLT, ONUs must share a single optical fiber trunk. Therefore Multi-Point Control Protocol (MPCP) is developed by IEEE 802.3ah task force to support a bandwidth allocation without collision among ONUs [4]. The MPCP is mainly operated by two control messages, GATE and REPORT. Each ONU informs OLT of the queue occupancy by REPORT to help the OLT make an efficient bandwidth allocation decision. The OLT assigns the transmission timeslot by GATE.

Several dynamic bandwidth allocation schemes such as gated, fixed, limited, constant/linear credit service schemes are

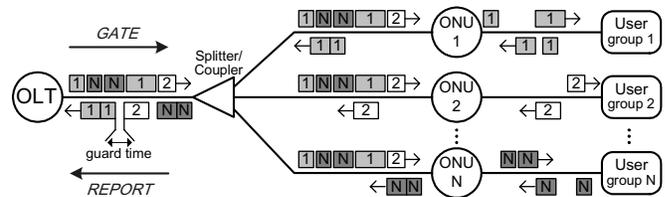


Fig. 1. Typical topology of EPON

suggested in Interleaved Polling with Adaptive Cycle Time (IPACT) [5]. They conclude that neither of the suggested service schemes is better than the limited service scheme. In this paper, we show that not only does limited service scheme suffer from utilization degradation under the non-uniform traffic, but also the degradation can be so severe when the number of ONUs, guard time and round-trip time increase. To resolve this problem, we propose a new scheme which relaxes maximum timeslot restriction and makes a bandwidth allocation decision considering other ONUs' queue occupancy. The proposed scheme can provide higher utilization than the conventional schemes and support max-min fairness under the non-uniform traffic.

The remainder of this paper is organized as follows. In section 2, the mechanism of GATE scheduling is given. In section 3, we present conventional and proposed bandwidth allocation schemes. In section 4 and 5, the utilization analysis and simulation results are provided to verify that our schemes perform well. Finally in section 6, we conclude the paper.

## II. GATE SCHEDULING

Assume that EPON has  $BW$  link capacity and consists of a OLT and  $ONU_i$ ,  $1 \leq i \leq N$ , where  $N$  is the total number of ONUs in the EPON. Every time the OLT receives REPORT containing a request (i.e., queue length) from  $ONU_i$ , it sends GATE containing the transmission *start time* and *duration* to  $ONU_i$  as follows.

- 1) Update  $SEI \leftarrow \max(SEI, now + RTT_i)$ .  
 $start\ time = SEI$ .

- 2) Decide the timeslot size  $G_i$  by the specific bandwidth allocation scheme.  
 $duration = G_i$ .
- 3) Update  $SEI \leftarrow SEI + G_i + r + g$ .
- 4) Send GATE to ONU $_i$ .

where  $now$  is the current time,  $RTT_i$  is the round-trip time for ONU $_i$  and  $SEI$  (Scheduling End-point Indicator) is the last point that has been allocated, that is, the earliest point that new allocation can be started. And  $r$  is the time required to send REPORT<sup>1</sup>,  $g$  is the guard time<sup>2</sup>. When ONU $_i$  receives GATE from the OLT, it sends data during the granted time  $G_i$  from *start time*, and then sends a new REPORT containing current queue length information  $R_i$  at the end of data transmission. If the OLT receives a new REPORT, it repeatedly does the GATE scheduling. In the ordinary case of  $SEI \geq now + RTT_i$ , the OLT allocates all the timeslots without omission. But in the case of  $SEI < now + RTT_i$ , the OLT cannot receive data from ONU $_i$  directly after current  $SEI$  even if the OLT sends GATE right now since the OLT must wait a previous REPORT to send a new GATE. Thus the  $SEI$  value is changed into  $now + RTT_i$  in step 1. Utilization degradation may happen because this operation makes an unallocated timeslot. We refer to this phenomenon as *RTT effect*.

### III. BANDWIDTH ALLOCATION SCHEMES

In this section, we describe conventional and proposed bandwidth allocation schemes. Fixed service scheme always grants the maximum timeslot size  $G_{max}$ . It is simple, but it does not consider the amount of traffic from each ONU. Limited service scheme grants as much as timeslot requested but it cannot exceed  $G_{max}$ ,  $G_i^{k+1} = \min(R_i^k, G_{max})$  where  $G_i^k$  and  $R_i^k$  denote the  $k$ th timeslot size for ONU $_i$  and the  $k$ th request from ONU $_i$  respectively. This scheme can achieve higher utilization, however, it may fail to fully utilize the bandwidth under the non-uniform traffic. Suppose that only one ONU wants to send data. The ONU can use  $G_{max}$  per every one cycle consisted of  $G_{max}$  and  $N$  number of guard time and report time. Therefore the utilization is limited to  $\frac{G_{max}}{G_{max} + N(r+g)}$ . This is because OLT cannot grant more than  $G_{max}$  even if other ONUs do not use any resources. We can expect utilization improvements if bandwidth allocation scheme can grant a timeslot more than  $G_{max}$  considering other ONUs' traffic.

#### A. Proposed Scheme 1 (P1)

We newly define a variable  $F_i^k$ , which indirectly indicates how much OLT can grant to ONU $_i$ . In the case of  $R_i^k > G_{max}$ , P1 guarantees at least  $G_{max}$  and efforts to grant  $R_i$  as much as possible but no more than  $F_i^k$ .

$$G_i^{k+1} = \begin{cases} R_i^k & \text{if } R_i^k \leq G_{max} \\ \max(G_{max}, \min(R_i^k, F_i^k)) & \text{otherwise} \end{cases} \quad (1)$$

where  $F_i^k = NG_{max} - \sum_{j=(i-N+1) \bmod N}^{(i-1) \bmod N} G_j$ .

<sup>1</sup>Fixed service scheme do not need REPORT message,  $r = 0$ .

<sup>2</sup>The guard time includes ONU's laser turn on/off time, OLT's receiver auto gain control settling time, and clock recovery time.

where  $G_i$  is the recently granted timeslot size to ONU $_i$ . The utilization will be improved by relaxing maximum timeslot  $G_{max}$  constraint. But P1 may cause fairness problem since it is possible to happen that an ONU, which originally has been using up  $NG_{max}$  timeslot, yields not  $\frac{NG_{max}}{2}$  but only  $G_{max}$  timeslot to a new coming ONU.

#### B. Proposed Scheme 2 (P2)

Now we propose a dynamic bandwidth allocation scheme to maximize utilization and also achieve max-min fairness. P1 uses the recently granted timeslot of other ONUs but P2 uses the recently requested queue length of other ONUs. To calculate fair distribution, if OLT sends GATES to all ONUs after the requests come from all ONUs, then the polling time will cause bandwidth waste. Therefore a scheme in which the OLT does not wait until all the requests are collected is preferable. The time before GATE is sent to ONU $_i$ ,  $M$  information (reported queue length from ONUs) in request table are not used, and the other  $(N - M)$  are already used, that is, new information has not arrived yet. OLT distributes  $NG_{max}$  max-min fairly among ONUs based on the  $N$  requests and sends GATE to ONU $_i$  with the amount of fair share of ONU $_i$  on the assumption that there is little difference between the already used  $(N - M)$  information and the new  $(N - M)$  information. P2 allocates a timeslot as follows.

$$G_i^{k+1} = \begin{cases} R_i & \text{if } s_i = 1 \\ \frac{NG_{max} - \sum_{j=1}^N s_j R_j}{N - \sum_{j=1}^N s_j} & \text{otherwise} \end{cases} \quad (2)$$

where  $s_j = \begin{cases} 1 & \text{if } \sum_{k=1}^N \min(R_j, R_k) \leq NG_{max} \\ 0 & \text{otherwise} \end{cases}$

where  $R_i$  is the recently request from ONU $_i$  and  $s_i$  indicates whether or not OLT grants a timeslot as much as ONU $_i$  requests.

### IV. PERFORMANCE ANALYSIS

In this section, we analyze the utilization performance of the fixed, limited and proposed schemes.

#### A. Utilization without considering RTT effect

Let  $I_i$  and  $O_i$  respectively denote the rate of input and output at ONU $_i$  normalized to EPON link rate. We will derive output rates  $\{O_i\}_{i=1,2,\dots,N}$  in terms of arbitrary input rates  $\{I_i\}_{i=1,2,\dots,N}$  without considering RTT effect. And then total link utilization will be  $U = \sum_{k=1}^N O_i$ .

1) *Fixed service scheme*: OLT always grants  $G_{max}$ , thus cycle time is equal to constant  $c = NG_{max} + Ng$ . The output rate can be calculated as

$$O_i = \min\left(I_i, \frac{G_{max}}{NG_{max} + Ng}\right) \quad (3)$$

and stable condition (i.e., the output rate is the same as the input rate for all ONU $_i$ ) is

$$I_i \leq \frac{G_{max}}{NG_{max} + Ng}, \quad \text{for all } i. \quad (4)$$

2) *Limited service scheme*: To determine whether  $s_i = 1$  or not, let us assume that  $s_i = 1$ . If we replace input rate  $I_k$  which is larger than  $I_i$  by  $I_i$ , or  $I'_k = \min(I_i, I_k)$ , then all ONUs will satisfy  $s_k = 1$ ,  $O'_k = I'_k$  for all  $k$ . Under changed input rates, the cycle time will be  $c' = \frac{N(r+g)}{1 - \sum_{k=1}^N I'_k}$  because the total input rate is equal to  $1 - \frac{N(r+g)}{c'}$ . In the limited service scheme, granted timeslot  $G_i$  must be smaller than  $G_{max}$ ,  $G_i = c'O_i = c'I_i \leq G_{max}$ . Therefore we can determine  $s_i$  as follows.

$$s_i = \begin{cases} 1 & \text{if } \frac{N(r+g)}{1 - \sum_{k=1}^N I'_k} I_i \leq G_{max} \\ 0 & \text{otherwise} \end{cases} \quad (5)$$

The cycle time is  $c = \frac{G_{max} \sum_{k=1}^N (1-s_i) + N(r+g)}{1 - \sum_{k=1}^N s_i I_i}$  because  $c = \sum_{k=1}^N G_k + N(r+g) = c \sum_{k=1}^N s_i I_i + G_{max} \sum_{k=1}^N (1-s_i) + N(r+g)$ . The output rate can be calculated as

$$O_i = \min \left( I_i, \frac{G_{max} (1 - \sum_{k=1}^N s_i I_i)}{G_{max} \sum_{k=1}^N (1-s_i) + N(r+g)} \right). \quad (6)$$

By using the cycle time and output rate, we can obtain mean granted timeslot size for ONU $_i$ ,  $G_i = cO_i$  and stable condition is given by

$$\frac{N(r+g)}{1 - \sum_{k=1}^N I_k} I_i \leq G_{max} \text{ for all } i. \quad (7)$$

3) *Proposed scheme 1 & 2*: The total utilizations of P1 and P2 are equal at the steady state even though  $O_i$  may be different from each other. Therefore we will consider only P2 in the following analysis. For every  $i$ , we set  $s_i = 1$  if  $\sum_{k=1}^N \min(I_i, I_k) \leq \frac{NG_{max}}{NG_{max} + N(r+g)}$ , otherwise  $s_i = 0$ . If there exists  $i$  such that  $s_i \neq 0$ , at least one ONU $_i$  is not satisfied even though OLT grants total  $NG_{max}$  per cycle. In this case, the cycle time will be  $c = NG_{max} + N(r+g)$ . Otherwise,  $c = \frac{N(r+g)}{1 - \sum_{k=1}^N I_k}$  because the total input rate is equal to  $1 - \frac{N(r+g)}{c}$ . The output rate can be calculated as

$$O_i = \min \left( I_i, \frac{\frac{G_{max}}{NG_{max} + r + g} - \sum_{k=1}^N s_k I_k}{N - \sum_{k=1}^N s_k} \right). \quad (8)$$

By using the cycle time and output rate, we can obtain mean granted timeslot size for ONU $_i$ ,  $G_i = cO_i$  and stable condition is given by

$$\sum_{k=1}^N I_k \leq \frac{NG_{max}}{NG_{max} + N(r+g)}. \quad (9)$$

4) *Utilization comparison under the uniform and non-uniform traffic*: To compare utilization of the fixed, limited and proposed schemes under the uniform and non-uniform traffic, we choose traffic rates of ONUs as ONU $_{1 \sim 30} : \text{ONU}_{31 \sim 32} = 1 : k$  where  $k$  is the non-uniformness parameter. Fig. 2 shows utilization of four schemes with  $k=1, 10, 100$ . Under the uniform traffic, that is  $k=1$ , four schemes have equal utilization. Actually the proposed schemes run almost the same

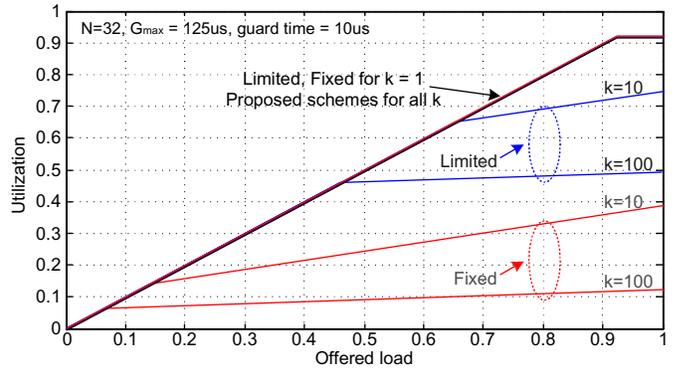


Fig. 2. Utilization comparison under the uniform and non-uniform traffic

as limited service scheme in this case. Note that utilization of conventional schemes decreases as non-uniformness  $k$  increases, however, the proposed schemes make it possible to get the same utilization as uniform traffic.

### B. Maximum Utilization without considering RTT effect

Now, let us find the maximum utilization when the offered load by ONUs except ONU $_1$  is  $0 \leq \rho \leq \frac{(N-1)G_{max}}{NG_{max} + N(r+g)}$ . This can be done by putting (10) into results of previous subsection.

$$I_1 = 1 - \rho \text{ and } \sum_{i=2}^N I_i = \rho, I_i = O_i \text{ for } i \neq 1 \quad (10)$$

Maximum utilization of fixed, limited and proposed schemes can be obtained as follows.

$$U_{Fixed} = \frac{G_{max}}{NG_{max} + Ng} + \rho \quad (11)$$

$$U_{Limited} = \frac{G_{max} + \rho N(r+g)}{G_{max} + N(r+g)} \quad (12)$$

$$U_{Proposed} = \frac{NG_{max}}{NG_{max} + N(r+g)} \quad (13)$$

### C. Maximum Utilization with considering RTT effect

In EPON, geographical distance from an OLT to ONUs can be from several kilometers to 20km [4] and round-trip time is not negligible. As seen in Fig. 3, RTT may cause waste of timeslot if condition (14) is satisfied. This is because OLT must wait a previous REPORT to send a new GATE.

$$\sum_{k \neq i} G_k + (N-1)r + Ng < RTT_i \quad (14)$$

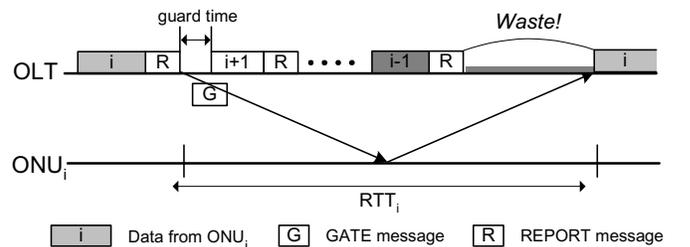


Fig. 3. RTT effect: timeslot waste due to round-trip time

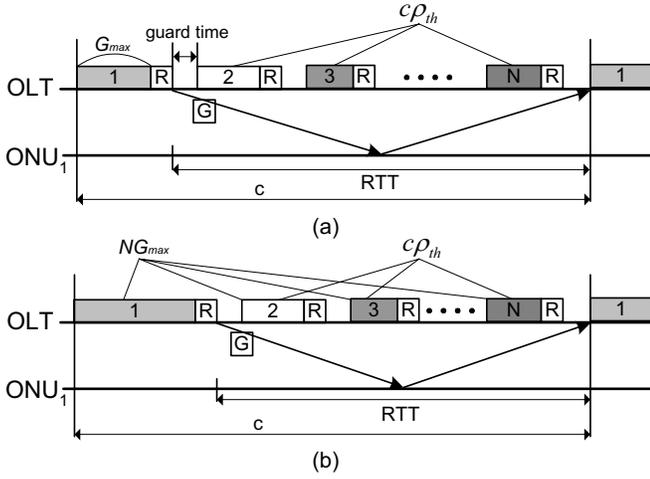


Fig. 4.  $\rho_{th}$  calculation (a) Limited service scheme, (b) Proposed schemes

In this case, maximum utilization is smaller than derivations (11)~(13), thus we need a modification. In this subsection, we will take RTT into consideration and derive maximum the utilization as offered load  $\rho$  by ONUs except ONU<sub>1</sub>.

1) *Fixed service scheme*: Fixed service scheme is not effected by RTT because it does not use REPORT. Therefore maximum utilization is same as previous derivation (11).

$$U_{Fixed} = \frac{G_{max}}{NG_{max} + Ng} + \rho \quad (15)$$

2) *Limited service scheme*: Maximum utilization will be achieved when ONU<sub>1</sub> uses up  $G_{max}$  per one cycle. To find a minimum offered load  $\rho_{th}$  to avoid RTT effect, we formulate following equations from Fig. 4(a).

$$RTT = c\rho_{th} + (N - 1)r + Ng \quad (16)$$

$$c = G_{max} + r + RTT \quad (17)$$

By using (16), (17), we can obtain  $\rho_{th}$  as follows.

$$\rho_{th} = \max\left(\frac{RTT - (N - 1)r - Ng}{G_{max} + r + RTT}, 0\right) \quad (18)$$

The maximum utilization is modified in the region of  $\rho \leq \rho_{th}$ .

$$U_{Limited} = \begin{cases} \frac{G_{max}}{G_{max} + r + RTT} + \rho & \text{if } \rho \leq \rho_{th} \\ \frac{G_{max} + \rho N(r + g)}{G_{max} + N(r + g)} & \text{if } \rho > \rho_{th} \end{cases} \quad (19)$$

3) *Proposed scheme 1 & 2*: Maximum utilization will be achieved when ONUs use up  $NG_{max}$  per one cycle. To find a minimum offered load  $\rho_{th}$  to avoid RTT effect, we formulate following equations from Fig. 4(b).

$$RTT = c\rho_{th} + (N - 1)r + Ng \quad (20)$$

$$c = NG_{max} + N(g + r) \quad (21)$$

By using (20), (21), we can obtain  $\rho_{th}$  as follows.

$$\rho_{th} = \max\left(\frac{RTT - (N - 1)r - Ng}{NG_{max} + N(r + g)}, 0\right) \quad (22)$$

The maximum utilization is modified in the region of  $\rho \leq \rho_{th}$ .

$$U_{Proposed} = \begin{cases} \frac{NG_{max}(1+\rho)}{NG_{max} + r + RTT} & \text{if } \rho \leq \rho_{th} \\ \frac{NG_{max}}{NG_{max} + N(r + g)} & \text{if } \rho > \rho_{th} \end{cases} \quad (23)$$

## V. SIMULATION RESULTS

In this section, we present simulation results using OPNET simulator [6] to verify the analysis and demonstrate the performance of proposed schemes. Fig. 5 shows simulation model. We generate the self-similar traffic by aggregating 32 pareto-distributed ON-OFF sources [7], [8]. And we generate Ethernet frames exponentially distributed with mean 500bytes from 64bytes to 1518bytes. Table I shows parameters used in this simulation.

TABLE I  
SIMULATION PARAMETERS

EPON Link rate ( $BW$ )	1Gbps
Number of ONUs ( $N$ )	8, 16, 32
Maximum timeslot ( $G_{max}$ )	125 $\mu$ s
Control message length ( $r$ )	0.512 $\mu$ s (=64bytes)
Guard time ( $g$ )	1, 5, 10 $\mu$ s
OLT/ONU queue size	300kbytes
Distance from OLT to ONUs	10km (RTT=100 $\mu$ s)

Fig. 6 depicts the maximum utilization versus network load (i.e., offered load by ONUs except ONU<sub>1</sub>). Fixed service scheme still grants the fixed timeslot  $G_{max}$  to every ONU even if network load is low. As a result, the maximum utilization is very low. Limited service scheme can achieve higher maximum utilization because ONU<sub>1</sub> gets chance to send data earlier as much as other ONUs do not use. However, the maximum utilization of the limited service scheme decreases as the non-uniformness increases (i.e. network load decreases), and moreover RTT effect prevents achieving high maximum utilization in the low offered load region ( $\rho < \rho_{th}$ ). For example, maximum utilization is very low in  $\rho < 0.34$  when  $N=16$ ,  $g=1\mu$ s. The proposed schemes can grant longer timeslot to ONU<sub>1</sub> by relaxing maximum timeslot restriction and making bandwidth allocation decision considering other ONUs' information, therefore we can always get full utilization regardless of the network load. In addition, the maximum utilization of conventional schemes decrease as the number of ONUs and guard time increases, but proposed schemes are almost independent of two variables.

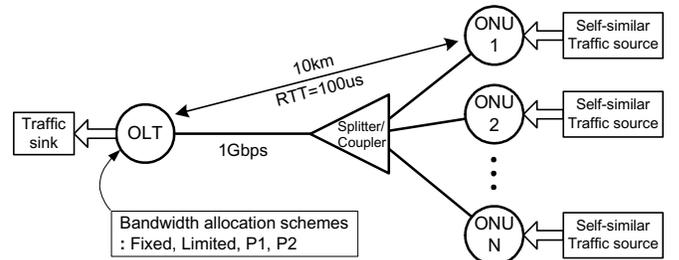


Fig. 5. Simulation model

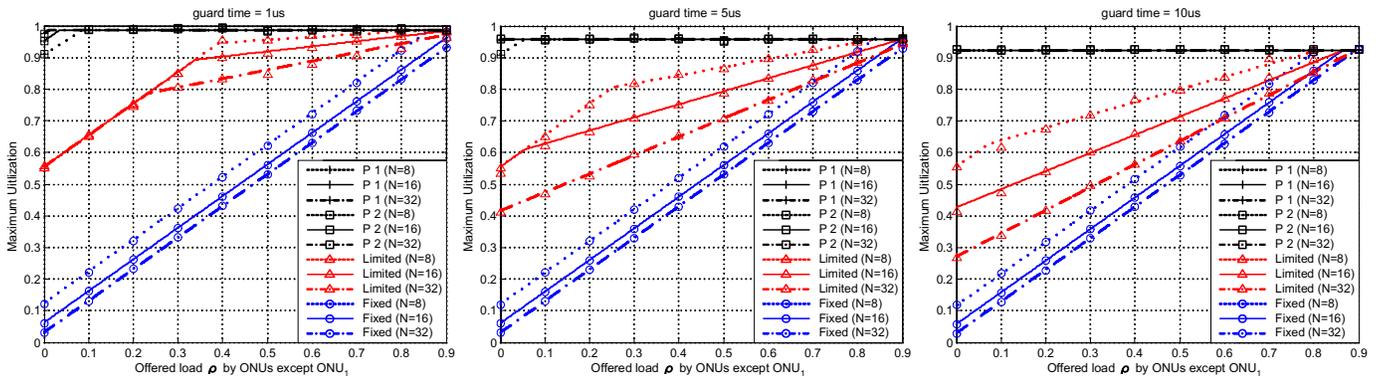


Fig. 6. Maximum utilization of different bandwidth allocation schemes versus offered load by ONUs except ONU<sub>1</sub> with the number of ONUs (N): (a) guard time = 1us, (b) guard time = 5us, (c) guard time = 9us (Line: Analysis, Symbol: Simulation)

TABLE II  
FAIRNESS SIMULATION SCENARIO AND RESULTS

	Arr. (sec)	Dept. (sec)	Input Rate (Mbps)	Output Rate (Mbps)			
				Fixed	Limited	P1	P2
ONU <sub>1</sub>	0	$\infty$	300	60	180	195	225
ONU <sub>2</sub>	10	$\infty$	300	60	180	255	225

## VI. CONCLUSION

In this paper, we point out the low utilization problem of the conventional bandwidth allocation schemes under the non-uniform traffic. To resolve this problem, we propose new schemes which relax maximum timeslot restriction and make intelligent bandwidth allocation decision using other ONUs' information. Our proposed schemes always utilize bandwidth more than 90% under any circumstances. Between two proposed schemes, P1 using previous GATE information may fail to guarantee fairness, however, P2 using previous REPORT information guarantees max-min fairness as well. Based on our analysis and simulation, we conclude that our proposed scheme (P2) always fully utilizes the bandwidth under the non-uniform traffic and guarantees max-min fairness.

## ACKNOWLEDGMENT

This work was supported in part by University IT Research Center Project and Electronics and Telecommunications Research Institute, Korea.

## REFERENCES

- [1] G. Pessavento and M. Kelsey, "PONs for the Broadband Local Loop," *Lightwave*, Vol.16, No.10, September 1999, pp.68-74.
- [2] B. Lund, "PON Architecture 'futureproofs' FTTH," *Lightwave*, Vol.16, No.10, September 1999, pp.104-107.
- [3] G. Kramer, G. Pessavento, "Ethernet Passive Optical Network (EPON): Building a Next-Generation Optical Access Network," *IEEE Communication Magazine*, Vol.40, Issue 2, February 2002, pp.66-73.
- [4] IEEE Draft P802.3ah™/D1.2, "Media Access Control Parameters, Physical Layers and Management Parameters for subscriber access networks," December 2002, <http://grouper.ieee.org/groups/802/3/efm>.
- [5] G. Kramer, B. Mukherjee, and G. Pessavento, "IPACT: A Dynamic Protocol for an Ethernet PON (EPON)," *IEEE Communication Magazine*, Vol.40, Issue 2, February 2002, pp.74-80.
- [6] OPNET Modeler 7.0, <http://www.opnet.com>.
- [7] W. Willinger, M. Taqqu, R. Sherman and D. Wilson, "Self-similarity through high-variability: stational analysis of Ethernet LAN traffic at the source level," *IEEE/ACM Transactions on Netwrking*, Vol. 5, Issue 1, February 1997, pp.71-86.
- [8] W. Leland, M. Taqqu, W. Willinger, and D. Wilson, "On the self-similar nature of Ethernet traffic (extended version)," *IEEE/ACM Transactions on Netwrking*, Vol. 2, Issue 1, February 1994, pp.1-15.

Fig. 7. Comparison of throughput of ONU<sub>1</sub> and ONU<sub>2</sub>

To observe the fairness performance of four schemes, we make simulation scenario as follows. ONU<sub>1</sub> sends traffic with 300Mbps from 0sec and ONU<sub>2</sub> starts to send 300Mbps at 10sec under 500Mbps background traffic by ONU<sub>3</sub>~ONU<sub>16</sub>. Fig. 7 compares throughput of ONU<sub>1</sub> and ONU<sub>2</sub>. Until 10sec, ONU<sub>1</sub> sends only 60Mbps and 260Mbps in the fixed and limited service scheme. But both P1 and P2 allow to send 300Mbps. After 10sec, throughput of ONU<sub>1</sub> and ONU<sub>2</sub> are 60Mbps in the fixed service scheme. In the limited service scheme, ONU<sub>1</sub> and ONU<sub>2</sub> get 180Mbps equally. ONU<sub>1</sub> and ONU<sub>2</sub> use 195+255=450Mbps in P1 which is 90Mbps higher than 180+180=360Mbps in the limited service scheme, however it is unfair. Unlike P1, ONU<sub>1</sub> and ONU<sub>2</sub> fairly use 225+225=450Mbps in P2.